



# **Year 3 Calculation and Bar Modelling Policy**

## Additive Reasoning

ELO: To add and subtract

MI: Add and subtract numbers mentally, including:

- A three-digit number and ones.
- A three-digit number and tens.
- A three-digit number and hundreds.

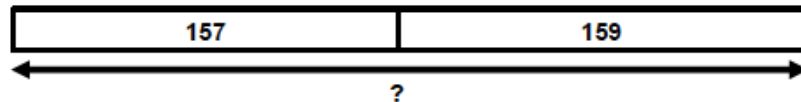
MI: Add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate.

MI: Estimate and use inverse operations to check answers to a calculation.

MI: Solve problems, including missing number problems, using number facts, place value and more complex addition and subtraction.

### Examples of adding:

Multilink/ Cuisenaire/Bar model



Abstract/Written Method/Language

In a cricket match, James' team score 157 runs in the first innings and 159 in the second innings. How many runs did they score in total?

$$157+159=$$

$$+ 157$$

$$\underline{159}$$

Multilink/ Cuisenaire/Bar model



Abstract/Written Method/Language

James scored 35 more points than Sam. Sam scored 167 points in his game. How many points did James score?

$$167+35=$$

$$+ 167$$

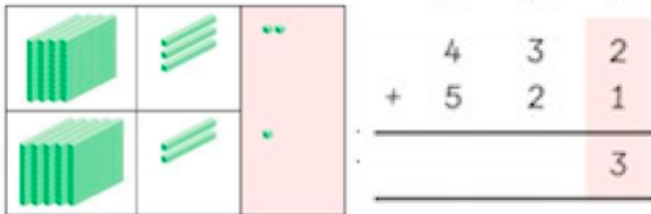
$$\underline{35}$$

## Examples of written methods for addition

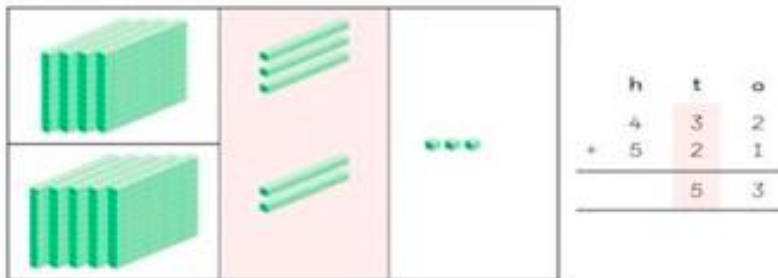
### Abstract/Written Method/Language

$$432 + 521 =$$

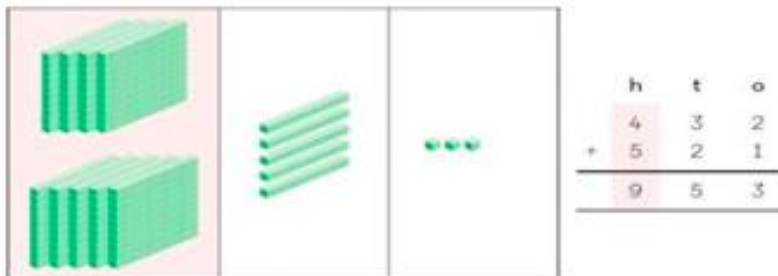
Step 1 Add the ones.  
2 ones + 1 one = 3 ones



Step 2 Add the tens.  
3 tens + 2 tens = 5 tens

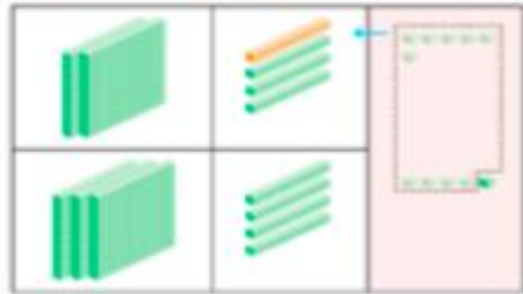


Step 3 Add the hundreds.  
4 hundreds + 5 hundreds = 9 hundreds



$$432 + 521 = 953$$

$$236 + 345 =$$



h	t	o
2	3	6
+ 3	4	5
	8	1

Step 2 Add the tens.  
 1 ten + 3 tens + 4 tens = 8 tens



h	t	o
2	3	6
+ 3	4	5
	8	1

Step 3 Add the hundreds.  
 2 hundreds + 3 hundreds = 5 hundreds

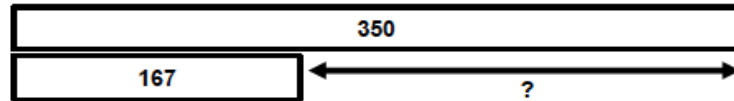


h	t	o
2	3	6
+ 3	4	5
5	8	1

$$236 + 345 = 581$$

## Examples of subtracting

Multilink/ Cuisenaire/Bar model



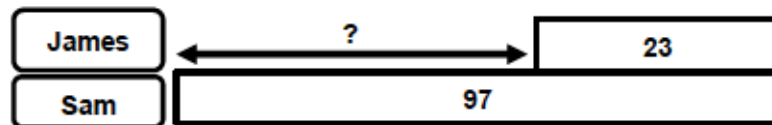
Abstract/Written Method/Language

There are 350 pages in Amber's book. On Tuesday, she reads 167 pages of her books. On Wednesday, she reads the rest of the book. How many pages did she read on Wednesday?

$$350 - 167 =$$

$$\begin{array}{r} - 350 \\ \underline{167} \end{array}$$

Multilink/ Cuisenaire/Bar model



Abstract/Written Method/Language

James has collected 23 fewer football stickers than Sam. Sam has collected 97. How many football stickers has James collected?

$$97 - 23 =$$

## Example of written method for subtraction

### Abstract/Written Method/Language

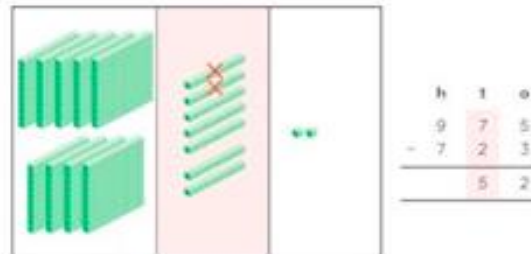
Only when secure with the method should exchanging be introduced.

Subtract 723 from 975.

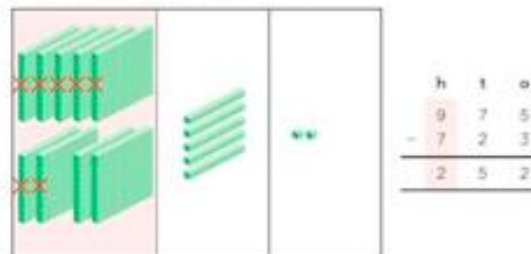
Step 1 Subtract the ones.  
5 ones - 3 ones = 2 ones



Step 2 Subtract the tens.  
7 tens - 2 tens = 5 tens



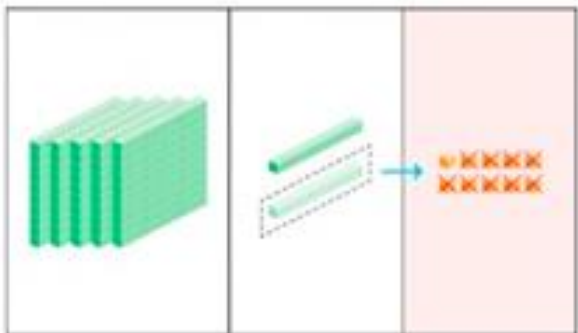
Step 3 Subtract the hundreds.  
9 hundreds - 7 hundreds = 2 hundreds



$$975 - 723 = 252$$

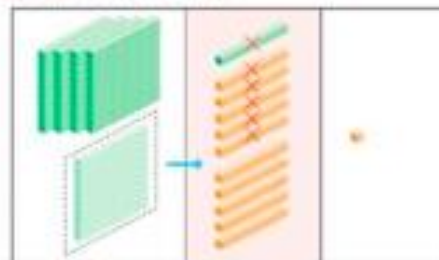
Subtract 269 from 520.

Step 1 Regroup 1 ten into 10 ones.  
Subtract the ones.  
10 ones - 9 ones = 1 one



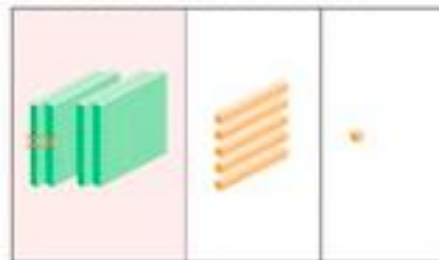
h	t
5	<del>2</del>
- 2	6

Step 2 Regroup 1 hundred into 10 tens.  
Subtract the tens.  
11 tens - 6 tens = 5 tens



h	t	o
<del>5</del>	<del>2</del> <sup>11</sup>	<del>9</del>
- 2	6	9
	5	1

Step 3 Subtract the hundreds.  
4 hundreds - 2 hundreds = 2 hundreds

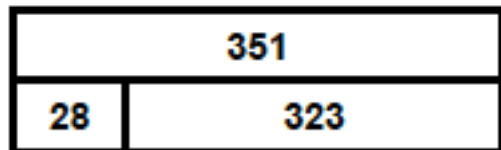


h	t	o
<del>5</del>	<del>2</del> <sup>11</sup>	<del>9</del>
- 2	6	9
2	5	1

520 - 269 = 251

**Examples of using the inverse to find the answer**

Multilink/ Cuisenaire/Bar model

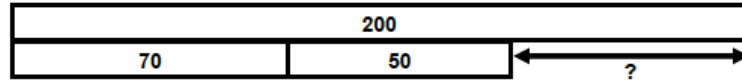


Abstract/Written Method/Language

For the calculation 323 + 28, Amber undertakes the calculation 351 - 323. Can you explain why she chose to do this?

### Examples of solving multi-step problems

#### Multilink/ Cuisenaire/Bar model



#### Abstract/Written Method/Language

Sally has £2 pocket money. She spends 70p on a comic and 50p on a bar of chocolate. How much change should she get?

### Multiplicative Reasoning

ELO: To multiply and divide

MI: Recall multiplication and division facts for multiplication tables up to  $12 \times 12$ .

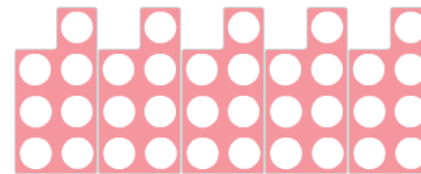
MI: Multiply two-digit and three-digit numbers by a one-digit number using formal written layout.

### Examples of multiplication and division

#### Concrete experiences

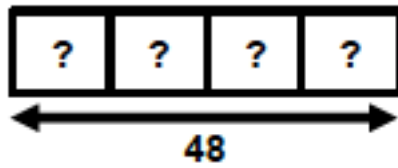
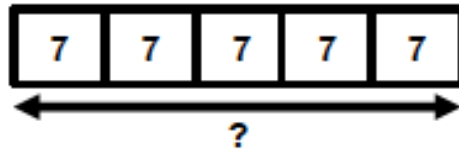


#### Numicon





Multilink/ Cuisenaire/Bar model



Abstract/Written Method/Language

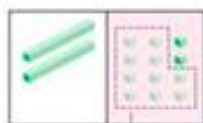
$$5 \times 7 = \underline{\quad}$$

$$4 \times \underline{\quad} = 48$$

## Example of written method for multiplication

### Let's Learn

- 1 There are 4 groups of 23 fish.  
How do we multiply 23 by 4?

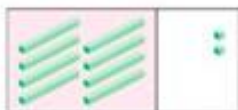


4 ones  $\times$  3 = 12 ones  
12 ones = 1 ten 2 ones



Step 1 Multiply the ones by 4.

$$\begin{array}{r} \text{t} \quad \text{o} \\ 2 \quad 3 \\ \times \quad 4 \\ \hline 1 \quad 2 \end{array}$$



2 tens  $\times$  4 = 8 tens



Step 2 Multiply the tens by 4.

$$\begin{array}{r} \text{t} \quad \text{o} \\ 2 \quad 3 \\ \times \quad 4 \\ \hline 1 \quad 2 \\ 8 \quad 0 \end{array}$$



12 + 80 = 92



Step 3 Add the products.

$$\begin{array}{r} \text{t} \quad \text{o} \\ 2 \quad 3 \\ \times \quad 4 \\ \hline 1 \quad 2 \\ + 8 \quad 0 \\ \hline 9 \quad 2 \end{array}$$

$$23 \times 4 = 92$$

There are 92 fish in 4 tanks.

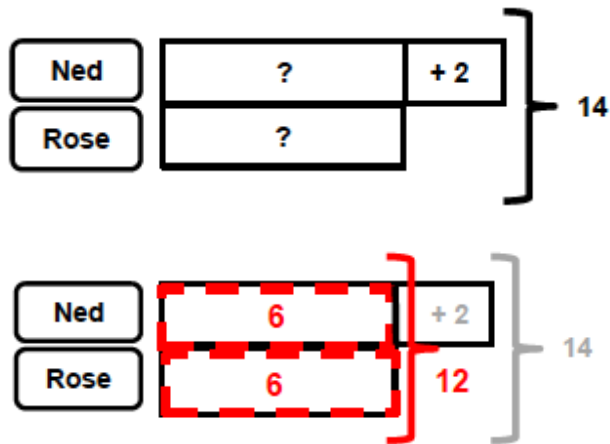
**Examples of solving problems, including missing number problems, involving multiplication and division**

ELO: To multiply and divide

MI: Recall multiplication and division facts for multiplication tables up to  $12 \times 12$ .

MI: Recognise and use the inverse relationship between multiplication and division and use this to check calculations and solve missing number problems.

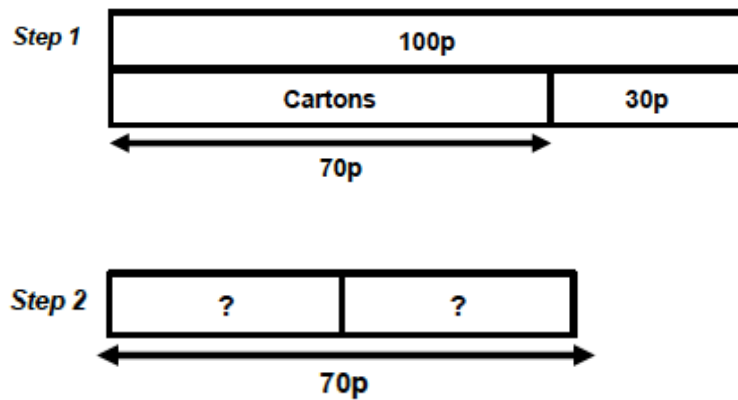
Multilink/ Cuisenaire/Bar model



Abstract/Written Method/Language

Ned and Rose have some biscuits. Altogether, they have 14 biscuits. Ned has 2 more biscuits than Rose. How many biscuits do they each have?

Multilink/ Cuisenaire/Bar model



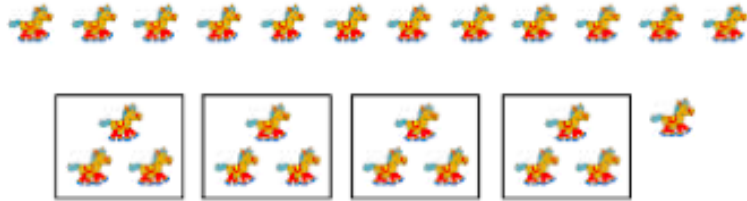
Abstract/Written Method/Language

I had one pound. I bought two cartons of drink and received 30p change. How much did each carton cost?

Year 3

## Examples of division with remainders

### Concrete experiences



### Numicon



### Multilink/ Cuisenaire/Bar model



### Abstract/Written Method/Language

$$13 \div 3 = 4 \text{ Remainder } 1$$

## Example of written method for division

Guidance Notes: Dividing using short division.

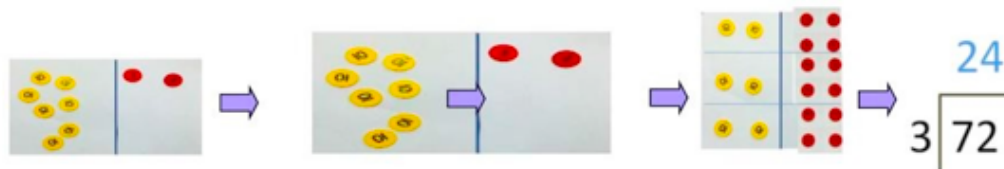
Once children are secure with division as grouping and demonstrate this using number lines, arrays etc., **short division** for larger 2-digit numbers should be introduced, initially with carefully selected examples requiring no calculating of remainders at all. Start by introducing the layout of short division by comparing it to an array.

$$\begin{array}{r} \text{T} \quad \text{U} \\ \hline 2 \quad 3 \\ 3 \overline{) 69} \\ \begin{array}{c} \color{red}{\bullet\bullet} \\ \color{red}{\bullet\bullet} \\ \color{red}{\bullet\bullet} \end{array} \quad \begin{array}{c} \color{green}{\bullet\bullet\bullet} \\ \color{green}{\bullet\bullet\bullet} \end{array} \end{array}$$

**Remind children of correct place value, that 69 is equal to 60 and 9, but in short division, pose:**

- How many 3's in 6? = 2, and record it above the **6 tens**.
- How many 3's in 9? = 3, and record it above the **9 ones**.

Once children demonstrate a full understanding of remainders, and also the short division method taught, they can be taught how to use the method when remainders occur within the calculation (e.g.  $72 \div 3$ ), and be taught to 'carry' the remainder onto the next digit.



### Examples of scaling problems and correspondence problems

ELO: To multiply and divide

MI: Solve problems involving multiplying and dividing, including using the distributive law to multiply two-digit numbers by one-digit, integer scaling problems and harder correspondence problems (such as n objects are connected to m objects).

Multilink/ Cuisenaire/Bar model

Abstract/Written Method/Language

Look at the bar model. What can you tell me?



Look at the bar model.  
What can you tell me?



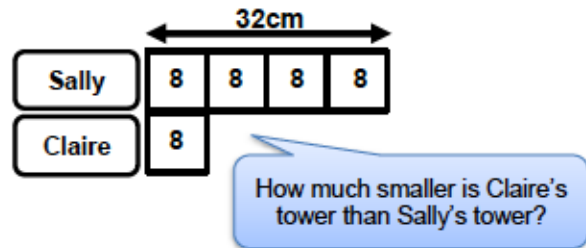
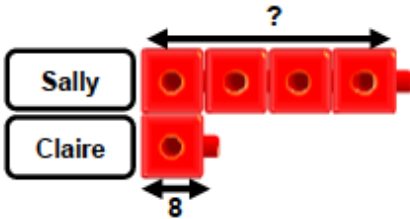
Can you change this model to show  
that C is four times as big as D?

Provide a speaking frame if  
required, for example:

.... is twice as many as ...  
... is three times as many as ...

Year 3

Multilink/ Cuisenaire/Bar model



Abstract/Written Method/Language

Claire builds a tower that is 8 cubes tall. Sally builds a tower that is 4 times as tall.

How tall is Sally's tower?

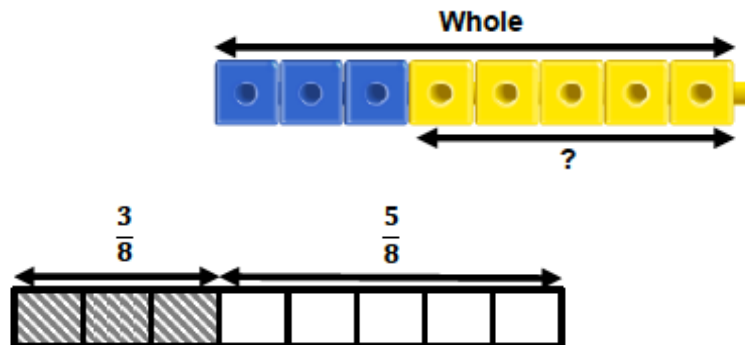
How much smaller is Claire's tower?

**Fractions**

ELO: To use fractions

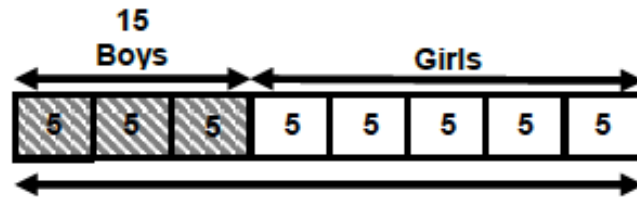
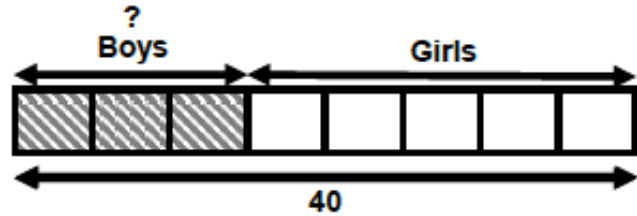
MI: Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators.

Multilink/ Cuisenaire/Bar model



Abstract/Written Method/Language

$\frac{3}{8}$  of a class are boys. What fraction of the class are girls?



If there are 40 children in the class, how many boys are there?

Equivalence

ELO: To use fractions

MI: Recognise and show, using diagrams, families of common equivalent fractions.

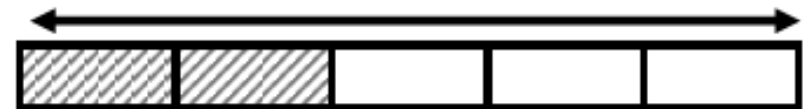
Guidance Notes:

Children could explore this with Cuisenaire rods first and then with bar models.

Multilink/ Cuisenaire

Bar Model

What does  $\frac{2}{5}$  look like as a bar model?



Year 3



Find equivalent fractions to  $\frac{2}{5}$



Always ensure the children reference 'the whole'

Let's split each of the fifths into two equal pieces. What does that look like?

